## DREYFOUS

Thematic guide

## MATH 7 DREYFOUS

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## Course Description

The main objective of the Math 7 course is to prepare the student with the necessary knowledge for the study of the Pre-Algebra course. The concepts studied in this course are fundamental to formalize the study of disciplines such as Geometry and Algebra, among others. This knowledge will allow students to continue to study mathematical subjects in greater depth, since learning these concepts will serve as a basis for the following grades. The contents of this course are aligned with the Estándares de contenido y expectativas de grado (2014) of the Puerto Rico Department of Education, as well as the United States Common Core State Standards. Students will make connections between the standards of the topics of algebra, numbering and operation, geometry, measurement, and data analysis. The pedagogical approach is focused on the teaching math for problem solving and the development of critical thinking skills as a means for the integral formation of the human being. The course emphasizes connecting curricular content to the solution of real-life problems so that the student finds relevance in the topics discussed and this awakens their interest in mathematics.

The Math 7 course includes topics that address standards such as: numerical and algebraic expressions, integers and rational numbers, equations and inequalities, ratios, proportions, percentages, relations and functions, plane and spatial geometry, measurement systems, data analysis, and probability.

The outline of objectives by lesson takes into consideration all the skills and concepts necessary for the student to establish the connections between the different standards in which mathematics is currently categorized. The general objectives contemplated in the Math 7 course are aligned with those of the Puerto Rico Department of Education, and allow for the transition between grade 6 and the Pre-Algebra course. Among them are:

1. To use the understanding of rational numbers, their properties and the order of operations to solve daily-life problems that includes various frameworks, such as financial decisions, calculation of distances and comparing temperatures.
2. To use ratios, proportions, and percentages to solve problems in everyday life such as calculating taxes, prizes, tips, and prices of items on sale.
3. To apply the order of operations to write, evaluate and simplify numerical expressions that model daily life situations and solve problems.
4. To identify the every-day relations that can be modeled with linear equations. The student will also be able to interpret what the slope and $Y$ intercept tells us about that relation.
5. To understand how to use the characteristics of two- and three-dimensional figures such as perimeter, area, surface and volume to describe and model the world around them.
6. Use statistical data in a critical manner, and critically analyze statistical information presented by others.
7. Represent and analyze daily life events using a probability model.

The teaching method focuses on conceptual understanding, skill development, and mathematical problem solving, together with the development of critical thinking skills, as a means for the integral formation of the student.

The course deliberately integrates content related to natural sciences, social sciences, technology and engineering, among others, with a double purpose: to encourage the student to see the direct application of what they learn and to visualize the importance of mathematics as a universal discipline at the service of society and its institutions. On the other hand, the incorporation of daily life situations and problems in each of the topics discussed aims to awaken the student's interest in the study of the discipline. The Math 7 course intends that the student understands the importance of mathematics, and knows how to use it in the decision making process to solve different kinds of problems, reaching their own conclusions. The student is expected to communicate appropriately using scientific and mathematical terminology, and to handle technology appropriately. Finally, it is expected that the student will be able to recognize the relevance of mathematics in personal and professional life.

## Course Structure

The Math 7 course consists of twelve units carefully subdivided into different lessons. The number of lessons per unit depends on the scope and depth with which the different topics are discussed and developed. Each lesson has an interactive presentation divided, in turn, into sections that present and explain the contents of the topic to be studied. Each presentation includes conceptual definitions, concrete examples, explanations, multiple representations, practice exercises, application of concepts and skills in everyday life.

In addition, the lessons include practice exercises, quizzes, additional practice labs, assignments, self-assessment exercises and a descriptive log with detailed information for the teacher, as well as a variety of internet links, among other resources. In turn, the lessons include worksheet assignments that reinforce the concepts studied in each lesson. The activities are varied and flexible, with the purpose of satisfying the particular needs and interests of each student. The practice and self-assessment activities seek to make the student aware of their strengths and weaknesses in the mastery of the content, with the purpose of them gradually taking control of their learning. The teacher, as an integral and essential part of the process, will have the responsibility of stimulating, orienting, guiding and periodically evaluating the learning achieved of each student.

The units are made up of the following parts:

## Lessons

Each unit is made up of different lessons, divided into topics, macro concepts and skills. In turn, each lesson consists of five key elements: course presentation or content, documents in digital format (PDF), internet links, self-assessment and descriptive Log.

- Lesson Content. Each lesson content presented contains a detailed explanation of the concepts and skills of the lesson as established in the objectives. In addition, it consists of the following elements that systematically contribute to the development of the desired learning in the student:
- Examples. In each section, when skills are developed, examples that explain
 step-by-step the solution to an exercise or problem are included, so that the student reviews the concepts and skills presented.
- Practice. This includes a series of carefully selected exercises in order for the student to practice the skills and concepts discussed. Its purpose is to
 periodically compare the learning achieved by the student before continuing with other subjects and skills. It does not include procedures or explanations; it only includes the solution of the exercises.
- Solution. It is used to hide the solution to an exercise or problem that the student should try to answer. Once you click on this icon, the solution or answer to the exercise will be displayed.
- Process. It is a button behind that brings up the steps or the algorithm to follow $\because$ when solving an exercise or problem.
- Demonstration / Steps. It presents formal demonstrations of the derivation of 5 important formulas or algorithms.
- Calculator. It includes the explanation of the processes when using and handling the calculator to solve the section's exercises. It also connects the student to the virtual graphing calculator.
- Animation. It gives access to explanations, procedures or graphics that visually show the concepts and skills discussed in the section. It ensures that the development and conceptual understanding of the student is looked after.
- Definition. It includes formal mathematical definitions of concepts and processes mentioned or discussed.
- Biography. Includes a short biography of the mathematician or scientist who is credited with developing the definition, formula, procedure, or demonstration used in the lesson.
- Note. This icon points out common errors or reinforces details that should not be forgotten.
- Did you know... This section presents an explanation or situation that connects aspects of everyday life with the mathematical skills and concepts discussed. In some cases, this section shows the link between the development of logical thinking in humans with certain mathematical skills and processes.
- Tabs. They are located on the right side of the presentation, and can be maroon
 or blue. They unfold to the left, and include flow charts, biographies, notes, photos, explanations, suggestions, reminders, Did you know... or necessary background knowledge.
- Incorrect. Indicates when the student has selected an incorrect answer in the
 included practice exercises.
- Correct. Indicates the correct selection to the answer of an exercise or practice problem.
- Photo or image. Connects a particular explanation to a photo or image.

- Video. It accesses a short video that links mathematical content to everyday life.

- Internet. It is a direct link to a site or Internet portal closely related to the topic.


Each of the sections included in the presentation is connected to a particular icon that identifies it, as shown in the explanation provided. In the initial presentations of the course the icon with the word that describes the section is included, this way the student will become familiar with what each of the icons represents. In subsequent presentations only the icon that accesses the section is included. In subsequent presentations only the icon that accesses to the section is included.

- PDF documents. These documents include a copy of practice exercises from the lesson, an additional practice section, activities that require the use of a calculator, or assignments. These documents can be printed out for the student to work on in pencil and on paper. Assignments are exercises and problems that the student works on at home, and that allow them, through practice, to strengthen the skills and concepts learned. Assignments are optional.
- Internet Links. These links are a direct connection to the Internet, and can be accessed directly from the presentation. They include additional explanations, examples, applications or demonstrations that allow students' conceptual development in the skills and topics discussed.
- Self-assessment. It consists of practice tests that the student answers to monitor their own learning before taking the formal unit evaluation tests offered by the teacher.
- Descriptive Log. This is the detailed lesson plan. This includes specific lesson objectives, standards and expectations, teaching strategies and resources, concepts, Internet links and references, among others. The only person with access to the descriptive logs will be the teacher.

Course Structure: Curricular Components


These develop the content through definitions, explanations, examples and demonstrations.


How Much Did I Learn?


Special sections


Short and objective exercises aimed at the evaluation and application of knowledge, located at the end of the development of the topics. Contains the solutions.

These broaden students' learning experiences. The lessons may have one or more They will be included where relevant. These sections are:


Research and Discover:
Research on additional topics or integration with other subjects.

Create and Build:
Applications of what has been learned and creation of projects.



By clicking the gray tab at the top or bottom right of some of the Lesson Content slides, the student will be able to see some important notes to reinforce or clarify the content, such as formulas or prior definitions.

| Button Directory |  |  |  |
| :---: | :---: | :---: | :---: |
| Navigation |  |  |  |
|  | Close |  | Credits |
|  | Solution |  | Return |
| Generals |  |  |  |
|  | Animation |  | Practice |
|  | Link |  | Reason |
|  | Definition |  | Review |
|  | Biography |  | Steps |
|  | Connect what you have learned |  | Graph |
|  | Image |  | Calculator |
|  | Note |  | Example |
|  | Diagram |  | Self-assessment. |
|  | Question |  | Process |



## Unit Breakdown

The titles of each unit will be detailed below, and the content of the units will be broken down into lessons with their titles, codes, objectives, topics, concepts and vocabulary.

## Unit 1. Numerical and Algebraic Expressions

At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Sets

## Code: C338G0SU01L01

## Objectives

At the end of the lesson the student will:

- identify the elements of a set.
- use the relevant concepts for sets, elements, and sub-sets.
- carry out joining and intersecting operations between sets.

Topics

- Symbols and Terminology
- Operations to combine sets*


## Concepts

- sets
- elements
- set operations
- union
- intersection
- subtraction
- complement
- subsets


## Vocabulary

- complement
- set
- element
- intersection
- subset
- union


## Lesson 2. Numerical and Geometric Patterns

## Code: C338G0SU01L02

## Objectives

At the end of the lesson the student will:

- identify numerical or geometric patterns.
- find the term or figure before or after in geometric numerical sequences.

Topics

- Patterns or Sequences
- Numeric Patterns
- Geometric patterns
Concepts
- geometric patterns
- numeric patterns
Vocabulary- pattern- sequence
Lesson 3. Powers and Square Roots
Code: C338G0SU01L03
Objectives
At the end of the lesson the student will:
- calculate the powers of integers
- determine the square root of perfect squares.
Topics
- Exponential Expression
- Properties of the Powers
- Square Roots
- Scientific Notation
Concepts
- scientific notation
- powers of a number
- square root
Vocabulary
- base
- exponential
- power
- root
Lesson 4. Numerical Expressions and Order of Operations
Code: C338G0SU01L04
Objectives
At the end of the lesson the student will:
- apply the order of operations to simplify algebraic expressions.
Topics- Numeric Expressions
- Order of Operations
Concepts
- order of operations
Vocabulary
- operations
Lesson 5. Algebraic Expressions and Evaluation
Code: C338G0SU01L05
Objectives
At the end of the lesson the student will:
- evaluate the algebraic expressions and apply the order of operations to simplifythem.
Topics
- Algebraic Expressions and Terms
- Evaluate Expressions
- Simplify Algebraic Expressions
- Verbal Expression to Algebraic Expression
Concepts- evaluate expressions
- verbal expression
- algebraic expressions
Vocabulary
- coefficient
- constant
- evaluation
- expression
- variable
Lesson 6. Properties of Real Numbers
Code: C338G0SU01L06
Objectives
At the end of the lesson the student will:
- sort the numbers into subsets of the actual numbers.
- identify the additive and multiplicative inverse and the identity element ofoperations between integers.
Topics
Set of real numbers
- Properties of Real Numbers
Concepts
- identity element
- inverse element
- associative property
- commutative property
- distributive property
Vocabulary
- associative
- commutative
- distributive
- identity
- inverse
Unit 2. IntegersAt the end of this unit the student will have completed the objectives found in the followinglessons:
Lesson 1. Absolute Value
Code: C338GOSU02L01
Objectives
At the end of the lesson the student will:
- define integers based on the concept of absolute value.
- determine the absolute value of integers.
Topics- Absolute Value and the Number Line
- Integers
Concepts- distance on the number line
- integer
- absolute value
Vocabulary
- distance
- integer
- absolute value
Lesson 2. Addition and Subtraction of Integers
Code: C338GOSU02L02
Objectives
At the end of the lesson the student will:
- add and subtract integers.
Topics
- Integers
- Sum of integers
- Subtraction of integers
Concepts
- subtraction
- sum
Vocabulary
- minuend
- opposite
- result
- subtrahend
Lesson 3. Multiplication and Division of Integers.
Code: C338GOSU02L03
Objectives
At the end of the lesson the student will:
- multiply and divide integers.
Topics
- Multiplying Integers
- Dividing Integers
Concepts
- dividing integers
- multiplying integers
Vocabulary
- quotient
- dividend
- divisor
- factors
- product
- remainder
Lesson 4. The Coordinates (Cartesian) Plane
Code: C338G0SU02L04
Objectives
At the end of the lesson the student will:
- identify in the coordinates plane the ordered pairs with integers.
Topics
- The Coordinates (Cartesian) Plane
- Points on the Coordinates Plane
Concepts
- horizontal and vertical coordinate
- point location
- ordered pairs
Vocabulary
- abscissa
- coordinate
- distance
- axis
- ordinate
- ordered pair
- plane
- points
Unit 3. Rational numbers
At the end of this unit the student will have completed the objectives found in the followinglessons:
Lesson 1. Rational numbers
Code: C338GOSU03L01
Objectives
At the end of the lesson the student will:
- identify the rational numbers
Topics
- Rational numbers
- Relation between Integers and Rational Numbers
- Fractions and Decimals
Concepts
- decimals
- numerator and denominator
- rational numbers
Vocabulary
- quotient
- decimal
- denominator
- numerator
- ratio
Lesson 2. Exact and Regular Decimals
Code: C338GOSU03L02
Objectives
At the end of the lesson the student will:
- differentiate between exact and periodic rational numbers.
- use the terminology to represent the periodic numbers.
Topics
- From Rational to Decimal
- From Decimal to Rational
- Periodic Decimals
Concepts
- decimal number
- periodic number
Vocabulary
- decimal
- periodic
Lesson 3. Compare and Order Decimals
Code: C338GOSU03L03
Objectives
At the end of the lesson the student will:
- compare and order the rational numbers in ascending and descending order.
Topics
- Order decimals in ascending order
- Order decimals in descending order
Concepts
- compare numbers
- greater than
- less than
Vocabulary
- ascending
- descending- greater than
- less than
Lesson 4. Homogeneous Fractions
Code: C338G0SU03L04
Objectives
At the end of the lesson the student will:
- perform the operations of addition, subtraction, multiplication, and division ofhomogeneous fractions.
Topics
- Addition and Subtraction of Homogeneous Fractions
- Multiplication of Homogeneous Fractions
- Division of Homogeneous Fractions
Concepts
- multiplying and dividing homogeneous fractions
- adding and subtracting homogeneous fractions
Vocabulary
- homogeneous
Lesson 5. Heterogeneous Fractions
Code: C338G0SU03L05
Objectives
At the end of the lesson the student will:
- perform the operations of addition, subtraction, multiplication, and division ofheterogeneous fractions.
Topics
- Addition and Subtraction of Heterogeneous Fractions
- Multiplying Heterogeneous Fractions
- Dividing Heterogeneous Fractions
Concepts
- multiplying and dividing heterogeneous fractions
- adding and subtracting heterogeneous fractions
Vocabulary
- heterogeneous
Lesson 6. Mixed Numbers
Code: C338G0SU03L06
Objectives
At the end of the lesson the student will:
- change from improper to mixed fraction and vice versa.
- perform the operations of addition, subtraction, multiplication, and division ofmixed numerals.
Topics
- From Improper Fraction to Mixed Number
- From Mixed Number to Improper Fraction
- Operations with Mixed Numbers
Concepts
- improper fraction
- mixed number
Vocabulary
- improper
- mixed
Lesson 7. Negative Exponents and Scientific Notation
Code: C338GOSU03L07
Objectives
At the end of the lesson the student will:
- apply the laws of exponents to simplify expressions with negative exponents.
- write the numbers in scientific notation.
Topics
- Negative Exponents and the Inverse Expression
- Simplify Algebraic Expressions.
- Expressing Numbers in Scientific Notation
Concepts
- negative exponents
- inverse expression
- scientific notation
Vocabulary
- exponent ..... - monomial


## Unit 4. Equations and Inequalities

At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Expressions and Equations

## Code: C338GOSU04L01

## Objectives

At the end of the lesson the student will:

- differentiate between an expression and an equation.
- evaluate the expressions and equations.

Topics

- Expressions or Equation
- Evaluate expressions
- Evaluate equations


## Concepts

- evaluation of expressions and equations
- equation solving

Vocabulary

- equation
- evaluation
- expression
- solution

Lesson 2. Equations with Addition and Subtraction
Code: C338G0SU04L02

## Objectives

At the end of the lesson the student will:

- solve degree equations with addition and subtraction.

Topics

- Solving Equations
- Solving Equations with Addition and Subtraction

Concepts

- solving equations

Vocabulary

- additive inverse
- solution


## Lesson 3. Equations with Multiplication and Division

## Code: C338G0SU04L03

## Objectives

At the end of the lesson the student will:

- solve first-degree equations with multiplication and division.


## Topics

- Solving Equations
- Solving Equations with Multiplication and Division


## Concepts

- solving equations

Vocabulary

- multiplicative inverse
- solution


## Lesson 4. Equations with Combined Operations

## Code: C338G0SU04L04

## Objectives

At the end of the lesson the student will:
solve first-degree equations with several operations.
Topics

- Solving Equations
- Solving Equations with Combined Operations


## Concepts

- solving equations
- solving combined equations


## Vocabulary

- additive inverse
- multiplicative inverse
- solution


## Lesson 5. Inequalities and Graphs

Code: C338G0SU04L05

## Objectives

At the end of the lesson the student will:

- interpret first-degree inequality and their graphs.

Topics

- First-Degree Inequalities**
- Solution Set
- Graphs of Inequalities


## Concepts

- solution set
- inequalities
- region

Vocabulary

- inequality
- region
Lesson 6. Inequalities with Addition and Subtraction
Code: C338GOSU04L06
Objectives
At the end of the lesson the student will:
solve first-degree inequalities with addition and subtraction.
- represent the solution set in set notation, interval, and in graph.
Topics
- Inequalities
- Solving Inequalities with Addition and Subtraction
- Graph of the Solution Set
Concepts
- solution set
- graph of the solution set
Vocabulary
- solution set
- infinite
- interval
- open interval
- closed interval
- semi-open interval
Lesson 7. Inequalities with Multiplication and Division
Code: C338G0SU04L07
Objectives
At the end of the lesson the student will:
- solve first-degree inequalities with multiplication and division.
- represent the solution set in set notation, interval, and in graph.
Topics
- Inequalities
- Solving Inequalities with Multiplication and Division
- Graph of the Solution Set
Concepts
- solution set
- graph of the solution set
Vocabulary
- solution set
- infinite
- interval
- open interval
- closed interval
- semi-open interval
Lesson 8. Inequalities with Combined Operations
Code: C338G0SU04L08
Objectives
At the end of the lesson the student will:
solve first-degree inequalities with combined operations.
- represent the solution set in set notation, interval, and in graph.
Topics
- Inequalities
- Solving Inequalities with Combined Operations
- Graph of the Solution Set
Concepts
- solution set
- graph of the solution set
Vocabulary
- solution set
- infinite
- interval
- open interval
- closed interval
- semi-open interval
Unit 5. Ratios and Proportionslessons:
Lesson 1. Ratios and Proportions
Code: C338GOSU05L01
Objectives
At the end of the lesson the student will:
- define ratio and proportion.
- determine the proportional ratios.
Topics
- Ratios
- Proportions
- Solving proportions
Concepts
- equivalent fractions
- proportion
- ratio
Vocabulary
- antecedent
- consequent
- proportion
- ratio
Lesson 2. Ratios and Unit Rates
Code: C338G0SU05L02
Objectives
At the end of the lesson the student will:
- determine the ratios and find the unit rates.
Topics
- Ratios and Rates
- Unit Rates
Concepts
- ratio
- rates
Vocabulary
- ratio
- rate
- unit
At the end of this unit the student will have completed the objectives found in the following
Lesson 3. Proportions
Code: C338GOSU05L03
Objectives
At the end of the lesson the student will:
- solve the proportions by applying cross-multiplication.
Topics
- Proportions
- Solving proportions
Concepts
- equivalent fractions
- proportions
- ratios
Vocabulary
- endsan
solution
Lesson 4. Similar figures
Code: C338G0SU05L04
Objectives
At the end of the lesson the student will:
- apply the concept of proportionality in similar figures.
Topics
- Similar figures
- Proportionality and Similar Figures
Concepts
- proportionality
- similarity
Vocabulary
- proportional
- similar
Lesson 5. Scales
Code: C338GOSU05L05
Objectives
At the end of the lesson the student will:
- apply the scales to everyday problems such as models and maps
Topics
- Scales
- Models and Maps
Concepts
- scales similarityVocabulary
- scale
- model
Unit 6. Percentage
At the end of this unit the student will have completed the objectives found in the followinglessons:
Lesson 1. Percentage
Code: C338GOSU06L01
Objectives
At the end of the lesson the student will:
- represent one percent of a relation.
Topics
- Concept of Percentage
- The Percent of an Amount
- Percentages Greater than 100\%.
Concepts
- percentage
- percent
Vocabulary- percent
Lesson 2. Fractions, Decimals, and Percent
Code: C338G0SU06L02
Objectives
At the end of the lesson the student will:
- calculate the equivalence between fractions, decimals, and percentages
Topics
- From Fraction to Percent
- From Decimal to Percent
- Equivalences between fraction, decimal, and percent
Concepts
- percentage
- percent proportion
Vocabulary
- percentage
- percentage
Lesson 3. Percent Proportions
Code: C338G0SU06L03
Objectives
At the end of the lesson the student will:
- use the proportions to calculate the percent and percentage.


## Topics

- Percentage Calculation
- Calculation of the Part
- Calculation of the Total

Concepts

- percent proportion


## Vocabulary

- percent proportion


## Lesson 4. Percentage Equation

Code: C338GOSU06L04

## Objectives

At the end of the lesson the student will:

- apply the percentage equation to everyday problems.

Topics

- Percentage Equation
- Calculation of the Part
- Calculation of the Whole

Concepts

- percentage equation

Vocabulary

- percentage


## Lesson 5. Percentage Change

Code: C338G0SU06L05

## Objectives

At the end of the lesson the student will:

- calculate the percentage change in everyday situations.


## Topics

- Percentage increase
- Percentage decrease

Concepts

- increase
- decrease
- percentage of change


## Vocabulary

- percentage change
Lesson 6. Percentage and Finances
Code: C338G0SU06L06
Objectives
At the end of the lesson the student will:
apply percentage in money and personal finance situations.
Topics
- Sales Tax
- Discounts on Purchases
- Simple Interest
Concepts
- calculate the increase
- calculate the decrease
- simple interest
Vocabulary
- interest


## Unit 7. Relations and Functions

At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Relations and Functions

## Code: C338G0SU07L01

## Objectives

At the end of the lesson the student will:

- define relation and function.
- identify whether a relationship is a function from the representation of sets, tables, graphs, ordered pairs, and verbal expressions.
Topics
- Relation and Function
- Domain and Range
- Evaluation of Functions and Graphs


## Concepts

- range
- domain
- function
- relation
- dependent variable
- independent variable

Vocabulary

- range
- domain
- function
- relation


## Lesson 2. Equations, Tables, and Graphs

## Code: C338G0SU07L02

## Objectives

At the end of the lesson the student will:

- establish the relationship between the equation, table of values, and graph of a numerical relation.


## Topics

- Table of Values
- Equations and Functions
- Function Graph


## Concepts

- equations
- function notation
- table of values


## Vocabulary

- table of values


## Lesson 3. Two-variable Equations and Graphs

Code: C338G0SU07L03

## Objectives

At the end of the lesson the student will:

- graph the relations of two variables on a coordinates plane.

Topics

- Two-variable Equations
- Graph of Two-variable Equations


## Concepts

- graphs of linear equations

Vocabulary

- abscissa
- ordinate


## Lesson 4. Constant rate of change

## Code: C338G0SU07L04

## Objectives

At the end of the lesson the student will:

- determine the rate of constant change of a linear function.

Topics

- Rate of Change
- Slope

Concepts

- horizontal rise
- vertical rise
- slope
- rate of change

Vocabulary

- slope
- rate of change


## Lesson 5. Straight Line Equation

Code: C338G0SU07L05

## Objectives

At the end of the lesson the student will:

- determine the equation of a line from the general information of the line, such as the slope and a point, or given two points.


## Topics

- General Equation of the Line
- Slope-intercept Equation
- Equation of the Line Given Two Points

Concepts

- slope-intercept equation
- Point-slope Equations

Vocabulary

- slope


## Lesson 6. Direct and Indirect Variation

## Code: C338G0SU07L06

## Objectives

At the end of the lesson the student will:

- determine whether a relation has a direct or inverse variation.


## Topics

- Direct variation
- Inverse variation


## Concepts

- constant variation
- direct variation
- indirect variation

Vocabulary

- reciprocal
- variation


## Lesson 7. Interpretation of Line Graphs

Code: C338G0SU07L07

## Objectives

At the end of the lesson the student will:

- interpret the line graphs in parts.


## Topics

- Graph Analysis
- Increasing, Decreasing, and Constant Intervals


## Concepts

- constant
- increasing intervals
- decreasing intervals


## Vocabulary

- constant
- increasing
- decreasing
Unit 8. Plane Geometry
At the end of this unit the student will have completed the objectives found in the followinglessons:
Lesson 1. Points, Lines and Planes
Code: C338GOSU08L01
Objectives
At the end of the lesson the student will:
- identify the basic elements of the geometry with the corresponding terminology: point, line, and plane
Topics- Geometry
- Points, Lines and Planes
Concepts
- collinear**
- distance between points
- terminology of points, lines and planes
- planes
- points
- lines
- relation between planes
- segments and rays
- types of lines
Vocabulary
- collinear**
- distance
- intersection
- plane
- point
- line
- segment
- ray
Lesson 2. Lines and segments (rays)
Code: C338G0SU08L02
Objectives
At the end of the lesson the student will:
- identify straight lines, segments, and rays with the corresponding terminology.
Topics
- The line
- Rays
- Segments
Concepts
- direction of the ray- operations with segments- relation between lines
Vocabulary
- intersection
- oblique
- parallels- Perpendicular- line- segment
- ray
Lesson 3. Distance Between two Points
Code: C338G0SU08L03
Objectives
At the end of the lesson the student will:
calculate the distance between two points on the coordinates plane.
Topics
- Distance Between Two Points on a Straight Line
- Distance Between Two Points in the Coordinates Plane
Concepts
- distance between points
- straight segment between two points
Vocabulary
- collinear
- distance
- Pythagorean theorem
Lesson 4. Angles
Code: C338G0SU08L04
Objectives
At the end of the lesson the student will:
- define and identify the angles with the corresponding terminology.
- Classify the angles according to their size.
Topics
- Definition of Angle
- Angle Classification
- Operations with Angles
Concepts
- angle classification
- acute
- right
- obtuse
- flat or straight
- angle measurement
- rotation of an axis


## Vocabulary

- acute
- angle
- degree
- flat*
- obtuse
- straight
- right
- rotation
- vertex


## Lesson 5. Relation Between Angles

## Code: C338G0SU08L05

## Objectives

At the end of the lesson the student will:

- carry out operations relating to complementary, supplementary, consecutive angles on a straight line, consecutive around a point, and opposed by the vertex.


## Topics

- Complementary and Supplementary Angles
- Consecutive Angles
- Angles Opposed by the Vertex


## Concepts

- angles around a point
- angles opposed by the vertex
- angles on a straight line
- complement of an angle
- sum of angles
- supplement of an angle
Vocabulary
- complementary
- opposite of the vertex
- supplementary
Lesson 6. Triangles and Quadrilaterals
Code: C338GOSU08L06
Objectives
At the end of the lesson the student will:
classify the triangles and quadrilaterals with their properties.
Topics
- The Triangle and its Classifications
- Properties of the Triangles
- Quadrilaterals and their classifications
- Properties of the Quadrilaterals
Concepts
- classifying of quadrilaterals
- classification of triangles according to angles
- classification of triangles by its sides
- diagonals of quadrilaterals
- sum of inner angles
Vocabulary
- acute
- square
- diagonal
- equilateral
- scalene
- isosceles
- obtuse
- rectangle
- rhombus
- rhomboid
- **trapezium
- trapezoid
Lesson 7. Transformations
Code: C338G0SU08L07
Objectives
At the end of the lesson the student will:- perform polygon transformations on the coordinates plane.
Topics
- Transformations
- Translations
- Reflections
- Rotations
Concepts
- horizontal reflection
- vertical reflection
- rotation- horizontal translation- vertical translation
Vocabulary
- axis of reflection
- degrees
- reflection
- rotation
- orbit
Lesson 8. Perimeter and Area
Code: C338G0SU08L08
Objectives
At the end of the lesson the student will:- calculate the perimeter and area of the triangles and quadrilaterals.
Topics- Concepts of Perimeter and Area
- Perimeter and Area of Triangles
- Perimeter and Area of Quadrilaterals
Concepts
- area
- calculation of area
- calculation of perimeter
- perimeter
Vocabulary
- height
- area
- base
- diagonal
- side
- perimeter
Lesson 9. Polygons
Code: C338G0SU08L09
Objectives
At the end of the lesson the student will:
- classify the polygons.- identify the congruence of the polygon and determine the similarity of thepolygons.
Topics
- Polygon Classification
- Polygon Consistency
- Similarity of Polygons


## Concepts

- polygon consistency
- irregular polygons
- regular polygons
- proportionality
- similarity of polygons
- sum of interior angles

Vocabulary

- interior angle
- congruence
- diagonal
- side
- Polygon
- proportionality
- similarity
- vertex


## Lesson 10. Circle and Circumference

## Code: C338G0SU08L10

## Objectives

At the end of the lesson the student will:

- define circumference and circle.
- identify the elements related to the circumference and circle.
- calculate the length of the circumference and the area of the circle.


## Topics

- Elements of the Circle
- Circumference
- Area of the Circle

Concepts

- area of the circle
- diameter
- length of the circumference


## Vocabulary

- arc
- center
- circle
- circumference
- chord
- diameter
- $\mathrm{pi}(\pi)$
- radius
- secant
- circular sector
- tangent
diameter


## Unit 9. Spatial Geometry

At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Polyhedron

## Code: C338GOSU09L01

## Objectives

At the end of the lesson the student will:

- classify the polyhedrons as prisms or pyramids.
- identify the elements of the prisms and pyramids.

Topics

- Polyhedron
- Prisms
- Pyramids

Concepts

- polyhedron classification
- pyramid classification
- prism classification


## Vocabulary

- edge
- base
- face
- pyramid
- polyhedron
- prisms
- projection
- vertex


## Lesson 2. Volume and Surface Area of Prisms

## Code: C338GOSU09L02

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of the prisms.

Topics

- Surface Area of Prisms
- Volume of Prisms

Concepts

- volume calculation
- sum of the area

Vocabulary

- height
- apothem
- area
- edge
- base
- face
- volume


## Lesson 3. Volume and Surface Area of Pyramids

## Code: C338G0SU09L03

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of the pyramids.
Topics
- Surface Area of Pyramids
- Volume of Pyramids
Concepts
- volume calculation
- sum of areas
Vocabulary
- height
- apothem
- area
- edge
- base
- face
- surface
- volume


## Lesson 4. Round Bodies

## Code: C338G0SU09L04

## Objectives

At the end of the lesson the student will:

- identify the round bodies and their elements.
Topics
- Round Bodies
- Cylinders
- Cones
- Spheres
Concepts
- characteristics of cylinders
- characteristics of cone
- characteristics of round bodies
- characteristics of spheres


## Vocabulary

- cylinder
- cone
- diameter
- sphere
- radius
- round


## Lesson 5. Volume and Surface Area of Cylinders

## Code: C338G0SU09L05

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of the cylinders.

Topics

- Surface Area of Cylinders
- Volume of Cylinders

Concepts

- cylinder surface area calculation
- cylinder volume calculation

Vocabulary

- height
- area
- base
- diameter
- radius
- surface
- volume


## Lesson 6. Volume and Surface Area of Cones

## Code: C338G0SU09L06

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of cones.

Topics

- Surface Area of Cones
- Volume of Cones

Concepts

- cylinder surface area calculation
- cylinder volume calculation

Vocabulary

- height
- area
- base
- diameter
- radius
- surface
- volume


## Lesson 7. Volume and Surface Area of Spheres

## Code: C338G0SU09L07

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of spheres.
Topics
- Surface area of Spheres
- Volume of Spheres
Concepts
- calculating the surface area of a sphere
- calculating the volume of a sphere
Vocabulary
- area
- diameter
- radius
- surface
- volume


## Lesson 8. Area and Volume of Composite Figures

## Code: C338G0SU09L08

## Objectives

At the end of the lesson the student will:

- calculate the surface area and volume of composite figures.
Topics
- Area of Composite Figures
- Volume of Composite Bodies
Concepts
- calculation of area
- volume calculation
- sum of volume
- addition and subtraction of areas


## Vocabulary

- area
- volume


## Unit 10. Measurement Systems

At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Customary System (English)

## Code: C338G0SU10L01

## Objectives

At the end of the lesson the student will:
recognize the units of measurement from the customary system (English)
Topics

- Units of Length
- Units of Weight
- Units of Capacity

Concepts

- capacity of a body
- length of a body
- weight of a body
- English measurement system


## Vocabulary

- capacity
- quartile
- gallon
- pound
- length
- measurement
- mile
- ounces
- weight
- foot (ft)
- inches
- cup
- ton
- yard


## Lesson 2. Metric System

## Code: C338GOSU10L02

## Objectives

At the end of the lesson the student will:

- recognize the units of measurement of the metric system.

Topics

- Units of Length
- Units of Weight
- Units of Capacity


## Concepts

- capacity of a body
- unit of measurement conversion
- length of a body
- weight of a body
- metric system of measurement


## Vocabulary

- centimeter
- gram
- kilogram
- kilometer
- liter
- meter
- milligram
- milliliter


## Lesson 3. Conversions in the Customary System

## Code: C338G0SU10L03

## Objectives

At the end of the lesson the student will:

- perform the conversions within the customary system (English).


## Topics

- Units of Length Conversion
- Units of Weight Conversion
- Units of Capacity Conversion


## Concepts

- equivalence of measures in the usual system


## Vocabulary

- capacity
- quartile
- gallon
- pound
- length
- measurement
- mile
- ounces
- weight
- foot (ft)
- inches
- cup
- ton
- yard
Lesson 4. Conversions in the Metric System
Code: C338GOSU10L04
Objectives
At the end of the lesson the student will:
- perform the conversions within the metric system.
Topics
- Units of Length Conversion
- Units of Weight Conversion
- Units of Capacity Conversion
Concepts
- equivalence of measures in the metric system
Vocabulary
- centimeter
- gram
- kilogram
- kilometer
- liter
- meter
- milligram
- milliliter
Lesson 5. Conversions Between the Customary and the Metric System
Code: C338G0SU10L05
Objectives
At the end of the lesson the student will:
perform the conversions between the metric and the customary (English) system.
Topics
- Units of Length Conversion
- Units of Weight Conversion
- Units of Capacity Conversion
Concepts
- measurement equivalences between the customary system and the metric system
Vocabulary
- conversion
- equivalence
- factor
Lesson 6. Conversion of Ratios, Areas, and Volumes
Code: C338G0SU10L06
Objectives
At the end of the lesson the student will:
- convert ratio, area and volume measurements between metric and customarymeasurement (English) systems.
Topics- Conversion of Units with Ratios
- Units of Area Conversion
- Units of Volume Conversion
Concepts
- equivalence of area
- equivalence of volume
- equivalent ratios
Vocabulary
- conversion factor
Unit 11. Data Analysis
At the end of this unit the student will have completed the objectives found in the followinglessons:
Lesson 1. Data Collection and Organization
Code: C338G0SU11L01
Objectives
At the end of the lesson the student will:
- identify data collection and organization strategies.
Topics
- Data Collection
- Frequency Table
- Stem-and-Leaf Display
Concepts
- data organization
- data collection
- data representation
Vocabulary
- data
- frequency
- gathering
- stem and leaf
Lesson 2. Data Representation and Graphs**
Code: C338G0SU11L02
Objectives
At the end of the lesson the student will:
- apply the different graphical representations of the collected data.
Topics
- Bar and Column Graph
- Line Graph
- Pie Chart
- Pictograph
Concepts
- data frequency
- drawing graphs
- maximum and minimum values
Vocabulary
- central angle
bar
- pie
- column
- axis
scale- maximum
- minimum
- picture- percent
Lesson 3. Stem-and-Leaf Display
Code: C338G0SU11L03
Objectives
At the end of the lesson the student will:
- construct stem-and-leaf displays for a data set.
Topics
- Stem-and-Leaf Display
- Analysis of a Stem-and-Leaf Display
Concepts
- graph construction
- graph interpretation
Vocabulary
- frequency
- maximum
- minimum
- stem and leaf
Lesson 4. Measures of Central Tendency
Code: C338G0SU11L04
Objectives
At the end of the lesson the student will:- identify and calculate measures of central tendency such as mode, median, andarithmetic mean (average).
Topics
- Mode
- Median
- Arithmetic Mean (Average)
Concepts
- arithmetic mean
- median
- measures of central tendency
- mode
Vocabulary
- median - summation
- mode - tendency
- average
Lesson 5. Quartiles and Percentiles
Code: C338G0SU11L05
Objectives
At the end of the lesson the student will:
identify the quartiles and percentiles of a data set.
Topics
- Distribution Measures
- Quartile
- Percentile
Concepts
- data analysis
- data set comparison
- data representation
Vocabulary
- quartile
- percentile
Lesson 6. Variation, Range, and Outliers
Code: C338G0SU11L06
Objectives
At the end of the lesson the student will:
- calculate the range of the data.
- compare two sets of data based on the variability or dispersion of the data.
- identify outliers in a data set.
Topics
- Range of Data
- Variability
- Atypical Value
Concepts
- data dispersion
- data distribution
Vocabulary
- atypical
- dispersion
- range
- variability
Lesson 7. Selecting the Best Graph
Code: C338G0SU11L07
Objectives
At the end of the lesson the student will:
- select the best graph to represent a data set.
- build different types of charts with all the elements identified.
Topics
- Types of Graphs
- Selecting the Best Graph
Concepts
- data analysis
- graphical display of data
Vocabulary
- bar
- pie
- column
- linear
- point
Lesson 8. Line of Best Fit
Code: C338G0SU11L08
Objectives
At the end of the lesson the student will:
draw the line that best fits a set of graphed data in the coordinates plane.
Topics
- Data Trend
- Line of Best Fit
- Data Interpretation and Range**
Concepts
- linear approximation*
- projections
- data trend
Vocabulary
- adjustment
- approximation
- increasing
- decreasing
- projection
- tendency

Unit 12. Probability
At the end of this unit the student will have completed the objectives found in the following lessons:

## Lesson 1. Probability of a Simple Event

## Code: C338GOSU12L01

## Objectives

At the end of the lesson the student will:

- determine the probability of a simple event.


## Topics

- Probability
- Probability of a Simple Event


## Concepts

- occurrence of an event
- probability of an event


## Vocabulary

- occurrence
- possibility
- probability


## Lesson 2. Probability and Sampling

## Code: C338GOSU12L02

## Objectives

At the end of the lesson the student will:

- establish the relationship between the sample and the probability of an event.


## Topics

- Population and Samples
- Sample Selection


## Concepts

- characteristics of the sample
- sample of the population
- types of samples


## Vocabulary

- random
- stratified
- sample
- population
Lesson 3. Counting
Code: C338GOSU12L03
Objectives
At the end of the lesson the student will:
- apply the theory of counting* and its relationship to the probability of an event.
Topics
- Counting Strategies
- Counting and Probability
Concepts
- counting methods
- probability of an event
Vocabulary
- counting
- probability
Lesson 4. Permutations
Code: C338GOSU12L04
Objectives
At the end of the lesson the student will:
- apply the permutations theory and its relationship to the probability of an event.
Topics
- Permutations
- Linear Permutation
- Circular Permutation
- Probability and Combinations
Concepts
- combinations
- permutations
Vocabulary
- combination
- factorial
- permutation
Lesson 5. Independent and Dependent Events
Code: C338GOSU12L05
Objectives
At the end of the lesson the student will:- differentiate between independent and dependent events.- calculate the probability of dependent and independent events.
Topics
- Probability of Independent Events
- Probability of Dependent Events


## Concepts

- dependent event
- independent event


## Vocabulary

- dependent
- independent


## Lesson 6. Theoretical and Experimental Probability

## Code: C338G0SU12L06

## Objectives

At the end of the lesson the student will:

- determine the theoretical and experimental probability of events.


## Topics

- Theoretical Probability
- Experimental Probability


## Concepts

- experimental probability
- theoretical probability


## Vocabulary

- experimental
- theoretical


## Lesson 7. Unbiased and Biased Sample

## Code: C338GOSU12L07

## Objectives

At the end of the lesson the student will:

- identify biased and unbiased samples.

Topics

- Biased Samples
- Unbiased Samples

Concepts

- unbiased samples
- biased samples

Vocabulary

- unbiased
- biased
Lesson 8. Predictions
Code: C338GOSU12L08
Objectives
At the end of the lesson the student will:- make predictions of events based on the calculation of probabilities or theinterpretation of the graph.
Topics
- Graph interpretation
- Predictions based on a Graph
Concepts
- data interpretation and graphs**
- making predictions
Vocabulary
- prediction

