## DREYFOUS \& ASSOCIATES <br> Course Overview

## Intermediate Algebra



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## Breakdown of Units

Below is an itemization of the division of each unit in lessons, including a detailed description of the general objectives and the name of each lesson with its corresponding objectives, concepts, and skills.

Unit 0. Cumulative review

Lesson 0. Cumulative review
Code: C302GOSU00LOO
Content.

- Cumulative Review U01-U04
- Cumulative Review U01-U05
- Cumulative Review U01-U06
- Cumulative Review U01-U09


## Unit 1. The Real Numbers

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 1. Numbers and Their Properties

Code: C302GOSU01L01

## Objectives

- Write a set of numbers using roster or set-builder notation.
- Write a rational number as a decimal.
- Classify a number as natural, whole, integer, rational, irrational, or real.
- Find the additive inverse of a number.
- Find the absolute value of a number.
- Given two numbers, use the correct notation to indicate equality or which is larger.
- Applications involving real numbers.


## Concepts

- absolute value of a number
- additive inverse of a number
- integer number
- irrational number
- natural number
- rational number
- real number
- roster
- set-builder notation
- whole number


## Lesson 2. Operations and Properties of Real Numbers

## Code: C302G0SU01L02

## Objectives

- Add, subtract, multiply, and divide signed numbers.
- Identify uses of the properties of the real numbers.
- Solve applications involving operations of real numbers.


## Concepts

- add
- divide signed numbers
- multiply
- real numbers
- subtract


## Lesson 3. Properties of Exponents

Code: C302GOSU01L03
Objectives

- Evaluate expressions containing natural numbers as exponents.
- Write an expression containing negative exponents as a fraction.
- Multiply and divide expressions containing exponents.
- Raise a power to a power and a quotient to a power.
- Convert between ordinary decimal notation and scientific notation, and use scientific notation in computations.


## Concepts

- negative exponents
- ordinary decimal notation
- quotient to a power
- scientific notation


## Lesson 4. Algebraic Expressions and the Order of Operations

## Code: C302G0SU01LO4

## Objectives

- Evaluate numerical expressions with grouping symbols.
- Evaluate expressions using the correct order of operations.
- Evaluate algebraic expressions.
- Use the distributive property to simplify expressions.
- Simplify expressions by combining like terms.
- Simplify expressions by removing grouping symbols and combining like terms.


## Concepts

- evaluate
- grouping symbols
- like terms
- numerical and algebra expression

Unit 2. Linear Equations and Inequalities
At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Linear Equations and Inequalities

Code: C302GOSU02LOO
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Linear Equations in One Variable

Code: C302GOSU02L01

## Objectives

- Determine whether a number is a solution of a given equation.
- Solve linear equations using the properties of equality.
- Solve linear equations in one variable involving fractions or decimals.
- Solve linear equations with one solution, no solutions, or infinitely many solutions.


## Concepts

- algebraic expression
- conditional equations
- constants
- equation
- terms
- variables


## Lesson 2. Formulas, Geometry, Problem Solving

Code: C302GOSU02LO2

## Objectives

- Solve a formula or literal equation for a specified variable and then evaluate the answer for given values of the variables.
- Translate from word expressions into mathematical expressions.
- Write a formula for a given situation that has been described in words.
- Solve problems about angle measures.


## Concepts

- angles
- area
- formula
- linear equation in one variable
- perimeter


## Lesson 3. Problem Solving Integers Geometry

Code: C302GOSU02L03

## Objectives

- Translate a word statement into a mathematical equation.
- Solve word problems of a general nature.
- Solve word problems about integers.
- Solve word problems about geometric formulas and angles.


## Concepts

- consecutive integer
- even and odd numbers
- word problem


## Lesson 4. Problem Solving: Percent, Investment, Motion And Mixture Problems

Code: C302GOSU02L04

## Objectives

- Solve percent problems.
- Solve investment problems.
- Solve uniform motion problems.
- Solve mixture problems.


## Concepts

- annual interest
- mixture
- percent
- uniform motion


## Lesson 5. Linear Compound Inequalities

## Code: C302GOSU02L05

## Objectives

- Graph linear inequalities.
- Solve and graph linear inequalities.
- Solve and graph compound inequalities.
- Translate sentences and solve applications involving inequalities.


## Concepts

- bounded and un bounded intervals
- compound inequalities
- intersection
- linear inequalities
- open and close intervals
- union


## Lesson 6. Absolute-Value Equations Inequalities

Code: C302GOSU02L06

## Objectives

- Solve absolute-value equations.
- Solve absolute-value inequalities of the form $|a x+b|<c$ or $|a x+b|>c$, where $c>0$.
- Solve applications involving absolute-value inequalities.


## Concepts

- absolute value
- distance


## Unit 3. Graphs and Functions

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Graphs and Functions

Code: C302GOSU03L00
UnitDocuments: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Graphs

Code: C302GOSU03L01

## Objectives

- Given an ordered pair of numbers, find its graph, and vice versa.
- Graph linear equations by finding solutions satisfying the equation.
- Graph lines by finding the $x$ and $y$ intercepts.
- Graph horizontal and vertical lines.
- Graph nonlinear equations by finding the solutions satisfying the equation.


## Concepts

- $x$ intercept
- $y$ intercept
- coordinate system
- equation
- graphs
- horizontal
- nonlinear
- ordered pair
- quadrants
- vertical

Lesson 2. Using Slopes to Graph Lines
Code: C302GOSU03L02

## Objectives

- Find the slope of a line passing through two given points.
- Use the definition of slope to decide whether two lines are perpendicular, parallel, or neither.
- Graph a line given its slope and a point on the line.
- Find the slope and $y$ intercept given the equation of a line.


## Concepts

- graphs
- intercept
- parallel
- perpendicular
- rate of change
- slopes
- two points


## Lesson 3. Equations of Lines

## Code: C302G0SU03L03

## Objectives

- Find the equation and the graph on a line given
- Two points.
- One point and the slope.
- The slope and the ${ }^{y_{\text {-intercept. }} \text {. }}$
- One point and the fact that the line is parallel or perpendicular to a given line.
- The slope is that of a horizontal or vertical line.


## Concepts

- horizontal line
- Intercept
- parallel
- perpendicular
- point - slope form
- slope
- slope intercept form
- vertical line

Lesson 4. Linear Inequalities in Two Variables
Code: C302GOSU03L04

## Objectives

- Graph linear inequalities.
- Graph inequalities involving absolute values.
- Solve applications involving linear inequalities.


## Concepts

- boundary line
- graphs
- inequalities
- linear inequalities
- shading
- solve applications


## Lesson 5. Introduction to Functions

Code: C302GOSU03L05

## Objectives

- Find the domain and range of a relation and determine whether the relation is a function.
- Use the vertical line test to determine if a relation is a function.
- Find the domain of a function defined by an equation.
- Find the value of a function.


## Concepts

- dependent variable
- domain
- equation
- function
- graphs
- independent variable
- mapping diagram
- range
- relation
- vertical line test

Lesson 6. Linear Functions
Code: C302G0SU03L06

## Objectives

- Identify linear and nonlinear functions from graphs or equations.
- Find the equation of a linear function from a graph.
- Use mathematical modeling with linearly related data.


## Concepts

- constant function
- increasing and decreasing function
- line of best fit
- linear function

Unit 4. Solving Systems of Linear Equations and Inequalities
At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Solving Systems of Linear Equations and Inequalities

Code: C302GOSU04L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Systems with Two Variables

Code: C302GOSU04L01
Objectives

- Find the solution of a system of two linear equations using.
- The graphical method
- The substitution method
- The elimination method
- Solve applications involving systems of equations


## Concepts

- consistent
- inconsistent
- system of equation

Lesson 2. Systems with Three Variables
Code: C302GOSU04L02

## Objectives

- Solve a system of three equations and three unknowns by the elimination method.
- Determine whether a system of three equations in three unknowns is consistent, inconsistent, or dependent.
- Solve applications involving systems of three equations.

Concepts

- consistent
- dependent
- inconsistent
- three equations

Lesson 3. Coin, Distance-Rate-Time, Investment, and Geometry Problems
Code: C302GOSU04L03

## Objectives

- Solve coin problems with two or more unknowns.
- Solve general problems with two or more unknowns.
- Solve rate, time, and distance (motion) problems with two or more unknowns.
- Solve investment problems with two or more unknowns.
- Solve geometry problems with two or more unknowns.
- Solve problems that can be modeled with a system.


## Concepts

- elimination method
- geometry
- substitution method
- systems
- unknowns


## Lesson 4. Systems of Linear Inequalities

## Code: C302GOSU04L04

## Objectives

- Graph systems of two linear inequalities.
- Graph systems of inequalities.


## Concepts

- graph
- inequalities
- solution set


## Unit 5. Polynomials

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Polynomials

Code: C302GOSU05L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Polynomials. Addition and Subtraction

Code: C302GOSU05L01
Objectives

- Classify polynomials.
- Find the degree of a polynomial and write in descending order.
- Evaluate a polynomial function.
- Add and subtract polynomials.
- Solve applications involving sums or differences of polynomials.


## Concept

- coefficient
- polynomials
- terms


## Lesson 2. Multiplication of Polynomials

Code: C302GOSU05L02

## Objectives

- Multiply a monomial by a polynomial.
- Multiply two polynomials.
- Use the FOIL method to multiply two binomials.
- Square a binomial sum or difference.
- Find the product of the sum and the difference of two terms.
- Use the ideas discussed to solve applications.


## Concepts

- FOIL
- monomial
- polynomials


## Lesson 3. The Greatest Common Factor and Factoring by Grouping

Code: C302GOSU05L03

## Objectives

- Factor out the greatest common factor of a polynomial.
- Factor a polynomial with four terms by grouping.


## Concepts

- factor
- polynomials


## Lesson 4. Factoring Trinomials

## Code: C302GOSU05L04

## Objectives

- Factor a trinomial of the form $x^{2}+b x+c$ ( $b$ and $c$ are integers).
- Factor a trinomial of the form $a x^{2}+b x+c$ using trial and error.
- Factor a trinomial of the form $a x^{2}+b x+c$ using the ac test.


## Concept

- factor tree
- factorization
- trinomial


## Lesson 5. Special Factoring

Code: C302G0SU05L05

## Objectives

- Factor a perfect square trinomial.
- Factor the difference of two squares.
- Factor the sum or difference of two cubes.


## Concepts

- cubes
- perfect square trinomial
- squares
- trinomial


## Lesson 6. General Methods of Factoring

## Code: C302GOSU05L06

## Objectives

- Factor a polynomial using the procedures given in the text.


## Concepts

- perfect square
- squares
- trinomial


## Lesson 7. Solving Equations by Factoring. Applications

Code: C302GOSU05L07

## Objectives

- Solve equations by factoring.
- Use the Pythagorean Theorem to find the length of one side of a right triangle.
- Solve applications involving quadratic equations.


## Concepts

- Pythagorean Theorem
- quadratic equations
- standard form
- zero product property


## Unit 6. Rational Expressions

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Rational Expressions

Code: C302GOSU06L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Rational Expressions

Code: C302G0SU06L01

## Objectives

- Find the values that make a rational expression undefined.
- Write an equivalent rational expression with the indicated denominator.
- Write a rational expression in one of the standard forms.
- Reduce a rational expression to lowest terms.


## Concepts

- denominator
- rational equation
- rational expression
- standard form
- undefined


## Lesson 2. Multiplication and Division of Rational Expressions

Code: C302GOSU06L02

## Objectives

- Multiply rational expressions.
- Divide rational expressions.
- Use multiplication and division together to simplify rational expressions.


## Concepts

- factor
- invert
- rational expression

Lesson 3. Addition and Subtraction of Rational Expressions
Code: C302GOSU06L03
Objectives

- Add and subtract rational expressions with the same denominator.
- Add and subtract rational expressions with different denominators.

Concepts

- expression
- last common denominator
- rational


## Lesson 4. Complex Fractions

Code: C302G0SU06L04

## Objective

- Write a complex fraction as a simple fraction in reduced form.

Concepts

- complex fraction
- denominator
- expression
- rational
- reciprocal


## Lesson 5. Division of Polynomials and Synthetic Division

Code: C302GOSU06L05

## Objectives

- Divide a polynomial by a monomial.
- Use long division to divide one polynomial by another.
- Completely factor a polynomial when one of the factors is known.
- Use synthetic division to divide a polynomial by a binomial.
- Use the remainder theorem to verify that a number is a solution of a given equation.


## Concepts

- monomial
- polynomial
- remainder
- synthetic division
- theorem


## Lesson 6. Equations Involving Rational Expressions

Code: C302GOSU06L06

## Objectives

- Solve equations involving rational expressions.
- Solve proportions.
- Solve applications involving proportions.


## Concepts

- expressions
- proportions
- rate/ratio
- rational


## Lesson 7. Applications. Problem Solving

Code: C302G0SU06L07

## Objectives

- Solve integer problems.
- Solve work problems.
- Solve distance problems.
- Solve for a specified variable.


## Concepts

- distance
- integer
- variable


## Lesson 8. Variation

Code: C302GOSU06L08
Objectives

- Write an equation expressing.
- Direct variation.
- Inverse variation.
- Joint variation.
- Solve applications involving direct, inverse, and joint variation.


## Concepts

- direct variation
- inverse variation
- joint variation


## Unit 7. Rational Exponents and Radicals

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Rational Exponents and Radicals

Code: C302GOSU07L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Rational Exponents and Radicals

Code: C302G0SU07L01
Objectives

- Find the $\boldsymbol{n}$ th root of a number, if it exists.
- Evaluate expressions containing rational exponents.
- Simplify expressions involving rational exponents.


## Concepts

- index
- principal root
- radical
- radicand
- rational exponents
- simplify

Lesson 2. Simplifying Radicals
Code: C302G0SU07L02
Objectives

- Simplify radical expressions.
- Rationalize the denominator of a fraction.
- Reduce the index of a radical expression.


## Concepts

- denominator
- fraction
- radical expressions
- rationalize

Lesson 3. Operations with Radicals
Code: C302GOSU07L03
Objectives

- Add and subtract similar radical expressions.
- Multiply and divide radical expressions.
- Rationalize the denominators of radical expressions involving sums or differences.


## Concepts

- add
- conjugate expression
- denominator
- like radical expressions
- rationalize
- subtract


## Lesson 4. Solving Equations Containing Radicals

## Code: C302GOSU07LO4

## Objectives

- Solve equations involving radicals.
- Solve applications involving radical equations.


## Concepts

- radical equations
- radical expressions


## Lesson 5. Complex Numbers

## Code: C302G0SU07L05

## Objectives

- Write the square root of a negative integer in terms of $i$.
- Add and subtract complex numbers.
- Multiply and divide complex numbers.
- Find powers of $\boldsymbol{i}$.


## Concepts

- complex numbers
- i
- negative integer
- pure imaginary numbers
- square root


## Unit 8. Quadratic Equations and Inequalities

At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Quadratic Equations and Inequalities

Code: C302G0SU08L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Solving Quadratics Completing Square

Code: C302G0SU08L01

## Objectives

- Solve quadratic equations of the form $a x^{2}+c=0$
- Solve quadratic equations of the form $a(x+b)^{2}=0$
- Solve quadratic equations by completing the square.
- Applications Involving Quadratic Equations.


## Concepts

- completing the square
- quadratics equations
- square root


## Lesson 2. The Quadratic Formula. Applications

## Code: C302GOSU08L02

## Objectives

- Solve equations using the quadratic formula.
- Solve factorable cubic equations.
- Solve applications involving quadratic equations.


## Concepts

- quadratic equations
- quadratic formula
- standard equations


## Lesson 3. Discriminant and Its Applications

Code: C302GOSU08LO3

## Objectives

- Use the discriminant to determine the number and type of solutions of a quadratic equation.
- Use the discriminant to determine whether a quadratic expression is factorable and then factor it.
- Find a quadratic equation with specified solutions.
- Verify the solutions of a quadratic equation.


## Concepts

- discriminant
- Non-real complex numbers


## Lesson 4. Solving Equations Quadratic Form

## Code: C302G0SU08L04

## Objectives

- Solve equations involving rational expressions by converting them to quadratic equations.
- Solve equations that are quadratic in form by substitution.


## Concepts

- extraneous solution
- rational expressions
- solve equations


## Lesson 5. Nonlinear Inequalities

## Code: C302G0SU08L05

## Objectives

- Solve quadratic inequalities.
- Solve polynomial inequalities of degree 3 or higher.
- Solve rational inequalities.
- Solve an application involving inequalities.


## Concepts

- critical values
- nonlinear inequalities
- polynomial inequalities
- quadratic inequalities

Unit 9. Quadratic Functions and the Conic Sections
At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Quadratic Functions and the Conic Sections

Code: C302GOSU01L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. Quadratic Functions (Parabolas) and Their Graphs

Code: C302GOSU09L01
Objectives

- Graph a parabola of the form $y=f(x)=a x^{2}+k$.
- Graph a parabola of the form $y=f(x)=a(x-h)^{2}+k$.
- Graph a parabola of the form $y=f(x)=a x^{2}+b x+c$.
- Graph a parabolas that are not functions with form $x=a(y-k)^{2}+h$ and $x=a y^{2}+b y+c$.
- Solve applications involving parabolas.


## Concepts

- applications
- downward
- graphs
- Parabolas
- Upward


## Lesson 2. Circles and Ellipses

Code: C302G0SU09L02

## Objectives

- Find the distance between two points.
- Find an equation of a circle with a given center and radius.
- Find the center and radius and sketch the graph of a circle when its equation is given.
- Graph an ellipse when its equation is given.
- Solve applications involving circles and ellipses.


## Concepts

- center
- circle
- ellipse
- equation
- graph
- radius


## Lesson 3. Hyperbolas and Identification of Conics

## Code: C302G0SU09L03

## Objectives

- Graph hyperbolas.
- Identify conic sections by examining their equations.


## Concepts

- conic
- ellipse
- Hyperbolas


## Lesson 4. Nonlinear Systems of Equations

## Code: C302GOSU09L04

## Objectives

- Solve nonlinear systems by substitution.
- Solve systems with two second degree equations by elimination.
- Solve applications involving nonlinear systems.


## Concepts

- nonlinear
- systems


## Lesson 5. Nonlinear Systems of Inequalities

Code: C302GOSU09L05

## Objectives

- Graph second-degree inequalities.
- Graph the solution set of a system of nonlinear inequalities.


## Concepts

- graph
- inequalities
- nonlinear

Unit 10. Functions-Inverse, Exponential, and Logarithmic
At the end of this unit the student will have completed the objectives found in the following lessons.

## Lesson 0. Functions—Inverse, Exponential, and Logarithmic

Code: C302GOSU10L00
Unit Documents: Collaborative Learning, Cumulative Review, Practice Test, PreTest, Research Questions, Review Exercises and Summary.

## Lesson 1. The Algebra of Functions

Code: C302G0SU10L01
Objectives

- Find the sum, difference, product, and quotient of two functions.
- Find the composite of two functions.
- Find the domain of $(f+g)(x),(f-g)(x),(f \circ g)(x)$, and $(f \div g)(x)$.
- Applications involving operations with functions.


## Concepts

- difference
- function
- product
- sum

Lesson 2. Inverse Functions
Code: C302G0SU10L02

## Objectives

- Find the inverse of a relation when the relation is given as a set of ordered pairs.
- Find the equation of the inverse of a relation.
- Graph a function and its inverse and determine whether the inverse is a function.
- Solve applications involving inverse functions


## Concepts

- difference
- function
- product
- relation
- sum


## Lesson 3. Exponential Functions

Code: C302GOSU10L03

## Objectives

- Graph exponential functions of the form $a^{x}$ or $a^{-x}(a>0$ and $a \neq 1)$.
- Determine whether exponential functions are increasing or decreasing.
- Solve applications involving exponential functions.


## Concepts

- applications
- constant
- decreasing
- exponential
- functions
- graph
- increasing


## Lesson 4. Logarithmic Functions and Their Properties

## Code: C302GOSU10L04

## Objectives

- Graph logarithmic functions.
- Write an exponential equation in logarithmic form and a logarithmic equation in exponential form.
- Solve logarithmic equations.
- Use the properties of logarithms to simplify logarithms of products, quotients, and powers.
- Solve applications involving logarithmic functions.


## Concepts

- logarithmic
- logarithmic equation
- logarithmic form


## Lesson 5. Common and Natural Logarithms

## Code: C302G0SU10L05

## Objectives

- Find common logarithms.
- Find natural logarithms.
- Change the base of a logarithm.
- Graph exponential and logarithmic functions base $e$.
- Solve applications involving common and natural logarithms.


## Concepts

- common logarithms
- graph
- logarithmic equation
- natural logarithms
- number $\boldsymbol{e}$
- power
- products
- quotients


## Lesson 6. Exponential and Logarithmic Equations and Applications

Code: C302GOSU10L06

## Objectives

- Solve exponential equations.
- Solve logarithmic equations.
- Solve applications involving exponential or logarithmic equations.

Concepts

- exponential
- logarithmic
- logarithmic equation

